

### **Section 3.1** Sequences and Limits

A sequence is a function defined on  $\mathbb{N} = \{1, 2, 3, \dots\}$  whose range is contained in  $\mathbb{R}$ .

We say that the sequence  $x_n$  converges to  $x$ , and write  $\lim_{n \rightarrow \infty} x_n = x$  or  $x_n \rightarrow x$ , if for all  $\epsilon > 0$ , there exists  $K(\epsilon)$  such that if  $n > K(\epsilon)$ ,  $|x_n - x| < \epsilon$ .