Math 305

Section 2.1 Differential Equations and Solutions

Definition An ordinary differential equation is an equation involving an unknown function of a single variable together with one or more of its derivatives.

Definition The <u>order</u> of a differential equation is the order of the highest derivative that occurs in the equation.

Definition A first order ordinary differential equation of the form y' = f(t, y) is said to be in <u>normal form</u>. Similarly, $y^{(n)} = f(t, y, y', \dots, y^{(n-1)})$ is the normal form for an nth order equation.

Definition A <u>solution</u> of the first order ordinary differential equation $\Phi(t, y, y') = 0$ is a differentiable function y(t) such that $\Phi(t, y(t), y'(t)) = 0$ for all t in the interval where y(t) is defined.

Definition A first order differential equation together with an initial condition,

$$y' = f(t, y), y(t_0) = y_0,$$

is called an initial value problem (IVP). A solution of an IVP is a differentiable function satisfying both the equation and the initial condition.

Definition The <u>interval of existence</u> of a solution to a differential equation is the largest interval over which the function is defined and remains a solution.