

## Math 201

### Section 6.3 Derivatives of Inverse Functions; Derivatives and Integrals Involving Exponential Functions

---

#### Differentiability of Inverse Functions

$$\frac{d}{dx}[f^{-1}(x)] = \frac{1}{f'(f^{-1}(x))}$$

Theorem Suppose that the domain of a function  $f$  is an open interval on which  $f'(x) > 0$  or on which  $f'(x) < 0$ . Then  $f$  is one-to-one,  $f^{-1}(x)$  is differentiable at all values of  $x$  in the range of  $f$ , and the derivative of  $f^{-1}(x)$  is given by the formula above.

#### Derivatives of Exponential Functions

$$\frac{d}{dx}[e^x] = e^x \quad \frac{d}{dx}[b^x] = \ln(b)b^x$$

#### Integrals Involving Exponential Functions

$$\int e^x dx = e^x + C \quad \int b^x dx = \frac{b^x}{\ln(b)} + C$$