Differential Equations Seminar: Week 4 Exercises

For each of the following systems, find and classify all equilibrium points:

1.
$$x' = 4 - 4x^2 - y^2$$
$$y' = 3xy$$

2.
$$x' = y^2 - 3x + 2$$
$$y' = x^2 - y^2$$

3.
$$xx'' + \frac{3}{2}(x')^2 = 1 - \frac{1}{x}$$
 (Hint: First rewrite this equation as a system.)